

L'exploitation  
et la maintenance  
des infrastructures



# Towards enriched mechanical models (modelling of discontinuities, crack initiation and deflection evolution)

## Models of structural deterioration

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## Models of structural deterioration

### Objectives:

Analyse the measurements of deflection basins in light of numerical mechanical modelling, in order to characterise the state of cracking of road pavement structures.

- Finite element approach: case of delamination and vertical cracking without propagation in 3D geometry
- Boundary element approach: case of 3D crack propagation

(<sup>1</sup>): P. Gaborit, Comportement thermo-mécanique de structures de chaussées bitumineuse (*thermo-mechanical behaviour of bituminous pavement structures*), PhD thesis, ENTPE, 2015

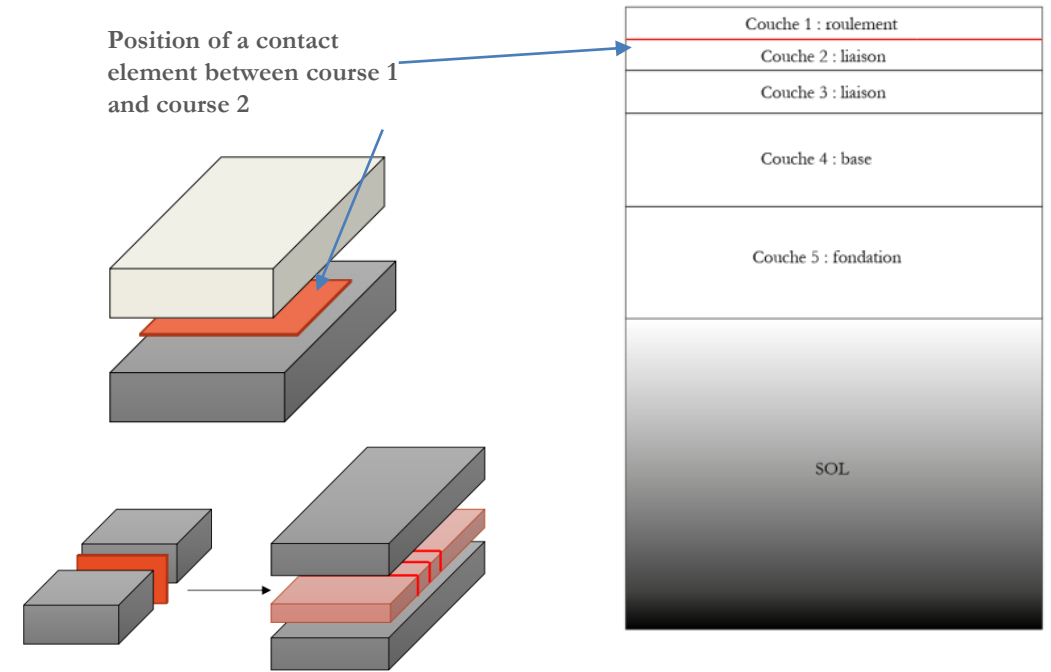


## ► Main deteriorations considered

- **Delamination between 2 courses** and opening of the interface. The surfaces considered can be large (**15 m<sup>2</sup>**) or small (**~ 1 m<sup>2</sup>**)
- Short (**1 m**) or long (**9 m**) **transverse** or **longitudinal** cracks with a spacing interval of 0.2 m
- Course thickness variation +/-1 cm

## ➤ Calculated deflections

- **Absolute deflection**
- **Simulation** of deflection measurement using a **curvometer**



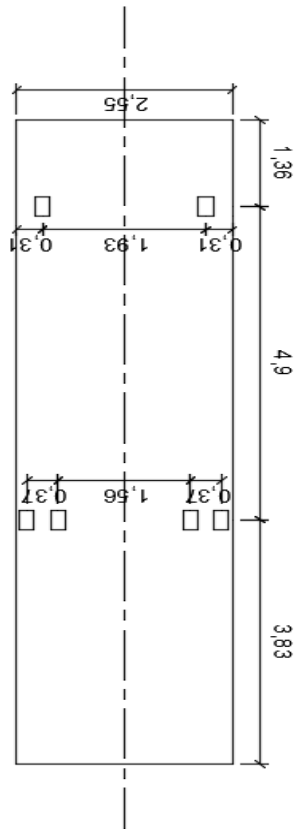
Road pavement layers	Wearing CoR (TAS)	Link 1 CL1 (BBG)	Link 2 CL2 (BBG)	Base CdB (BBG)	Foundation CdF (BBG)	Soil (PF3)
Thickness [m]	0.04	0.04	0.05	0.10	0.11	3.00
Behaviour	Elastic	Elastic	Elastic	Elastic	Elastic	Elastic
E [MPa]	4581	4581	4581	5174	13680	120
$\nu$	0.35	0.35	0.35	0.35	0.35	0.25

TABLE 1: CHARACTERISTICS OF THICK ASPHALT ROAD PAVEMENTS. CoR to Bond: data taken from the standard, Base - Foundation: values deduced from complex modulus tests. Temperature and frequency measured under loading: 17°C and 8.1 Hz

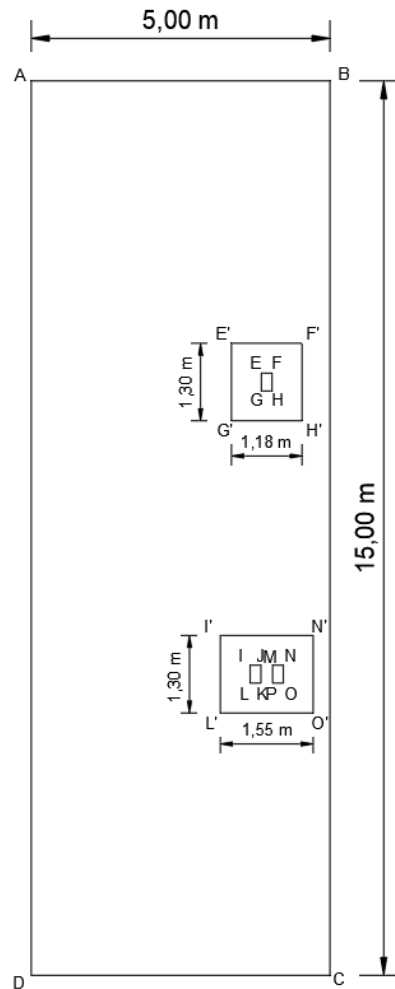
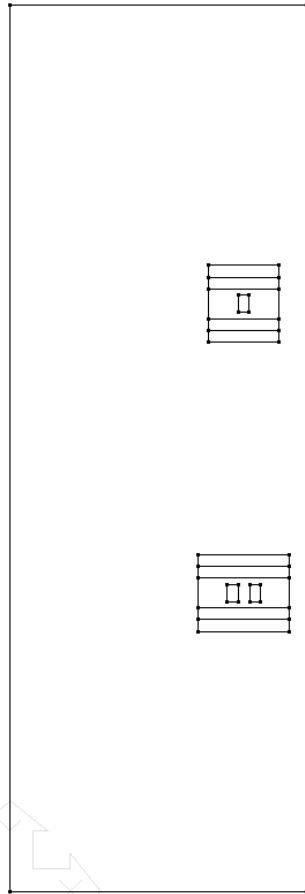


## ► Curvometer type loading

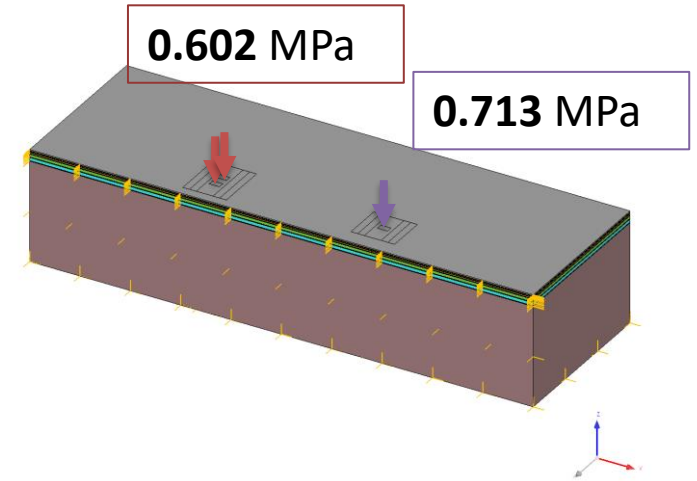
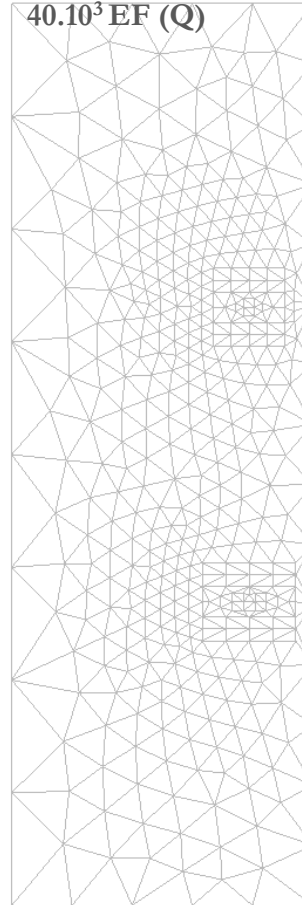
Loading diagram  
 (top view)



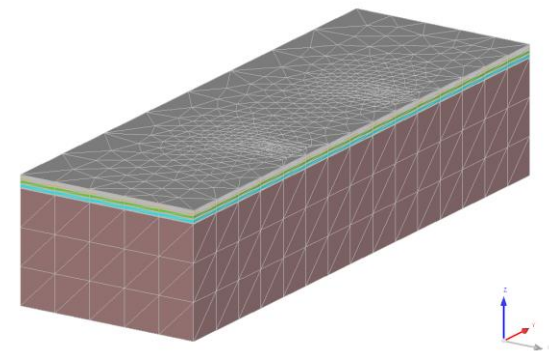
Geometry



Load  
 distribution  
 $40 \cdot 10^3 \text{ EF (Q)}$



Surface area of each tyre  
 ( $0.18 \cdot 0.3 \text{ m}^2$ )



## ► Comparison Alizé - César (EF) Thick asphalt road pavement

Maximum deflection (mm)	Alizé [transversal]	CESAR [transversal]	Alizé [longitudinal]	CESAR [longitudinal]	Alizé-César spread [transversal]	Alizé- César spread [longitudinal]
Without delamination	-0.2277	-0.2230	-0.2115	-0.2061	2%	3%
CoR_L1(*)	-0.2530	-0.2452	-0.2337	-0.2260	3%	3%
L1_L2(*)	-0.2800	-0.2687	-0.2622	-0.2506	4%	4%
L2_Base(*)	-0.3135	-0.2973	-0.2997	-0.2818	5%	6%
Foundation_Base(*)	-0.3263	-0.3083	-0.3145	-0.2944	6%	6%

\* With complete delamination of the interface (5\*15 m<sup>2</sup>)

## Characteristics of the interface with perfect sliding (César (EF))

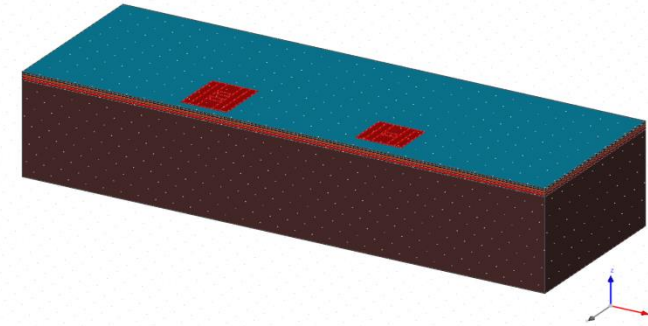
Sliding interface	RT	E
CoR – Link 1	1 MPa	4581 MPa
Link 1 – Link 2	1 MPa	4581 MPa
Link 2 – Base	1 MPa	4581 MPa
Base - Foundation	1 MPa	5174 MPa

- We note that the ALIZE model corresponds to our modelling using the CESAR (EF) software.

- The perfect sliding of the ALIZE software corresponds to a sliding surface with a tensile strength coefficient **RT= 1MPa** (tensile opening limit) and a **Young's modulus** equal to the **smallest modulus of two courses in contact**.

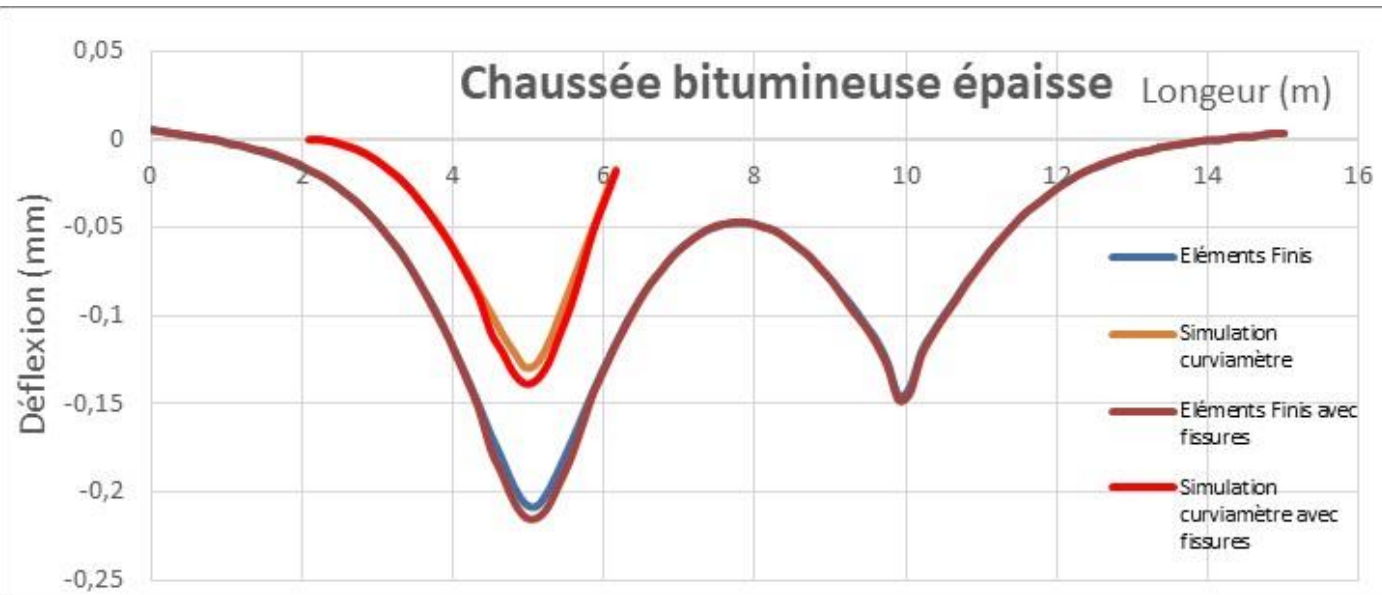
- Reduced sliding surface (1.3\*1.18 m<sup>2</sup>) and interface without resistance

Sliding interface with opening	
RT	E
1 kPa	1 MPa



Interface	Maximum deflection (mm)	
	César (EF) [transversal]	Increase/without delamination
Without delamination	-0.223	-
CoR – Link 1	-0.353	+56.88%
Link 1 – Link 2	-0.316	+40.44%
Link 2– Base course	-0.302	+34.22%
Base course – Foundation	-0.272	+20.88%

- ▶ Thick bituminous structure.  
Simulation of deflection basins using a curvometer calculation.



Deflection basins derived from the finite element calculation and simulation of the basin using a curvometer type calculation. (short longitudinal cracks)

Position of the 6 short longitudinal cracks	Transverse axis (EF)	Longitudinal axis (EF)	Curvometer (longitudinal calculation)
	$w_{max}$ [mm]	$w_{max}$ [mm] / relative deviation from non-cracked case	$w_{max}$ [mm] / relative deviation from non-cracked case
No cracks	0.226	0.209	0.130
Wearing course	0.229	0.215 / 2.9%	0.139 / 6.9%
Link 1	0.231	0.213 / 1.9%	0.136 / 4.6%
Link 2	0.235	<b>0.232 / 11%</b>	<b>0.156 / 20%</b>
Base	0.245	<b>0.227 / 8.6%</b>	<b>0.149 / 14%</b>
Foundation	0.247	<b>0.232 / 11%</b>	<b>0.156 / 20%</b>

Summary of calculated maximum vertical displacements ( $w_{max}$ ) (finite elements and curvometer) in absolute values for the thick bituminous pavement

Position of the 6 long longitudinal cracks	Transverse axis (EF)	Longitudinal axis (EF)	Curvometer (longitudinal calculation)
	$w_{max}$ [mm]	$w_{max}$ [mm] / relative deviation from non-cracked case	$w_{max}$ [mm] / relative deviation from non-cracked case
No cracks	0.226	0.209	0.130
Wearing course	0.263	0.216 / 3.3%	0.140 / 7.7%
Link 1	0.262	0.247 / 18.2%	0.171 / 31.5%
Link 2	0.260	<b>0.244 / 16.8%</b>	<b>0.168 / 29%</b>
Base	0.259	<b>0.241 / 15.3%</b>	<b>0.165 / 26.9%</b>
Foundation	0.265	<b>0.250 / 19.6%</b>	<b>0.174 / 33.8%</b>



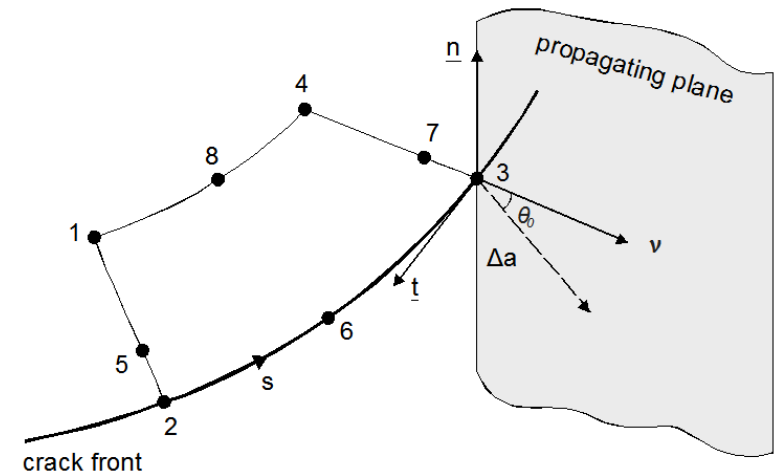


## ► 3D propagation of crack networks

- Developments are carried out using the Boundary Element Model
  - **Great flexibility in structuring 3D geometries**
  - Highly **accurate** determination of singular fields in **the vicinity of cracks**
  - Linking with the fast multipole method to set up a structural calculation code for **3D elasticity** and **3D fracture mechanics**.
- Paris law

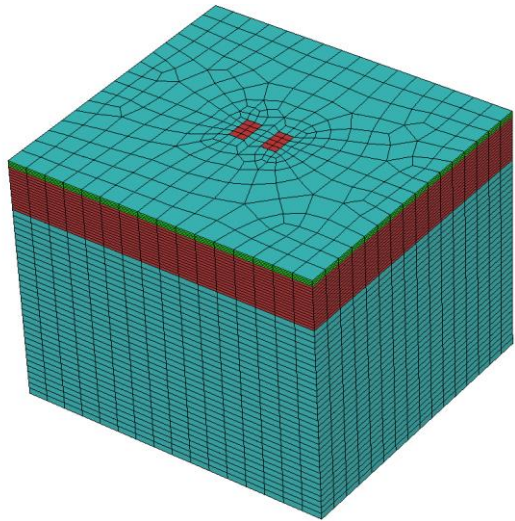
$$\frac{da}{dN} = A \cdot \Delta K^m \quad \Delta K = K_{\max} - K_{\min}$$

- The stress intensity factors at node 2 are determined for **propagation modes I, II, III**
- **The angle of propagation** is given by the criterion of the maximum tangential stress



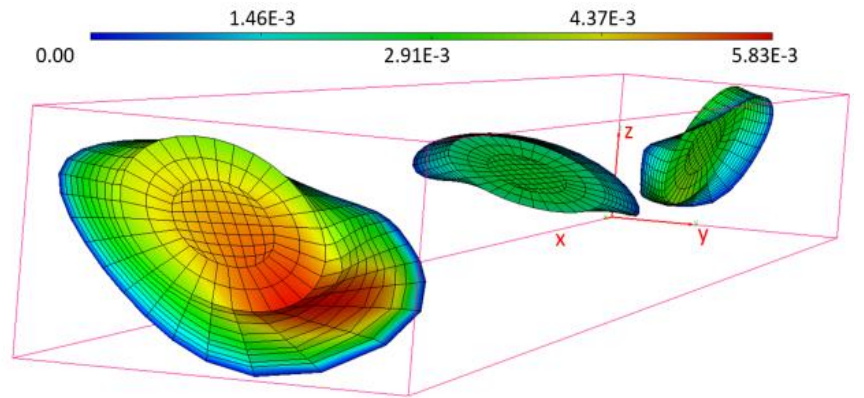
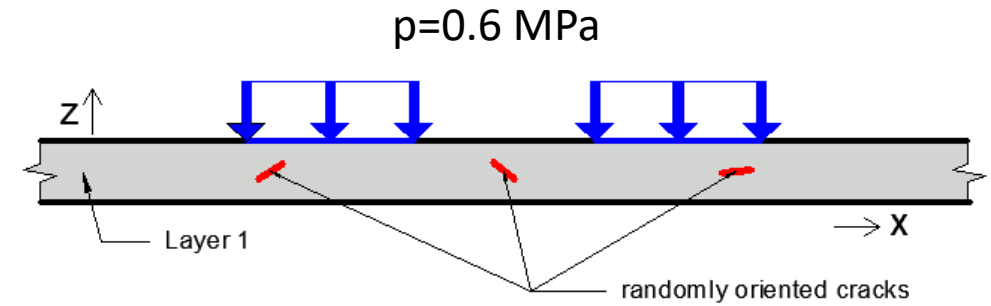
## ► Simulation of a road pavement with internal cracks

	Thickness (mm)	E (MPa)	$\nu$
Wearing course	66	6610	0.35
Granular course	500	180	0.30
Soil	2220	80	0.25



#	$N_c$	$N_{init}$	$N_{end}$	$T_{pre}(s)$	$T_{sol}(s)$	$T_{tot}(s)$
1	1	15 441	18 033	201	667	883
2	3	17 559	25 335	345	1 382	1 749
3	5	19 677	32 637	1 241	3 166	4 434

Calculation time for 1, 3 and 5 cracks



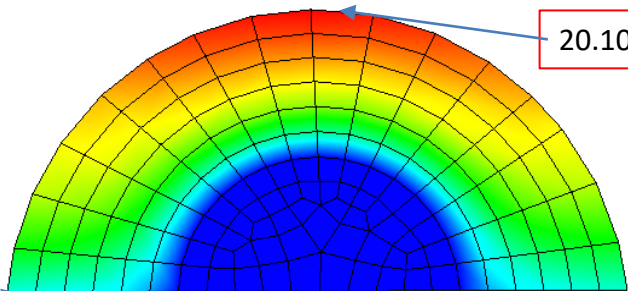
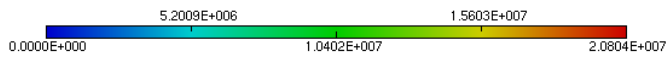
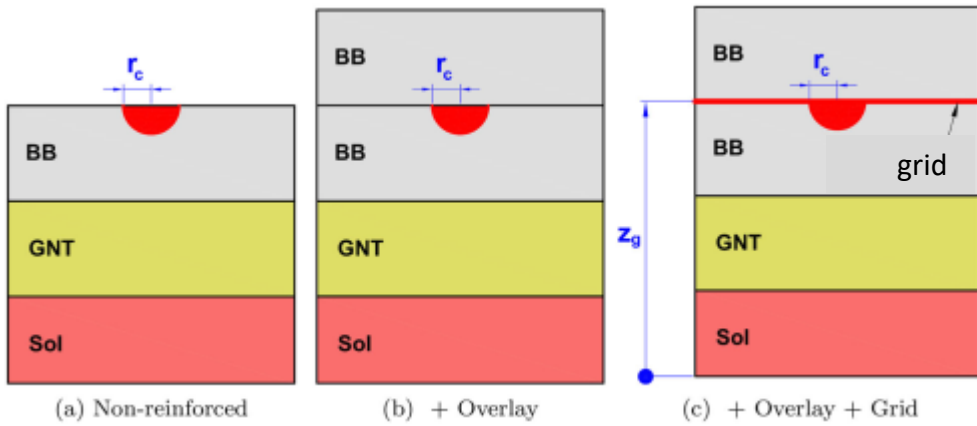
Shape of three cracks (diameter 20 mm) after propagation (crack opening in mm)

3D load distribution and pairing footprints:  $2 * (0.18\text{m} * 0.3\text{m})$





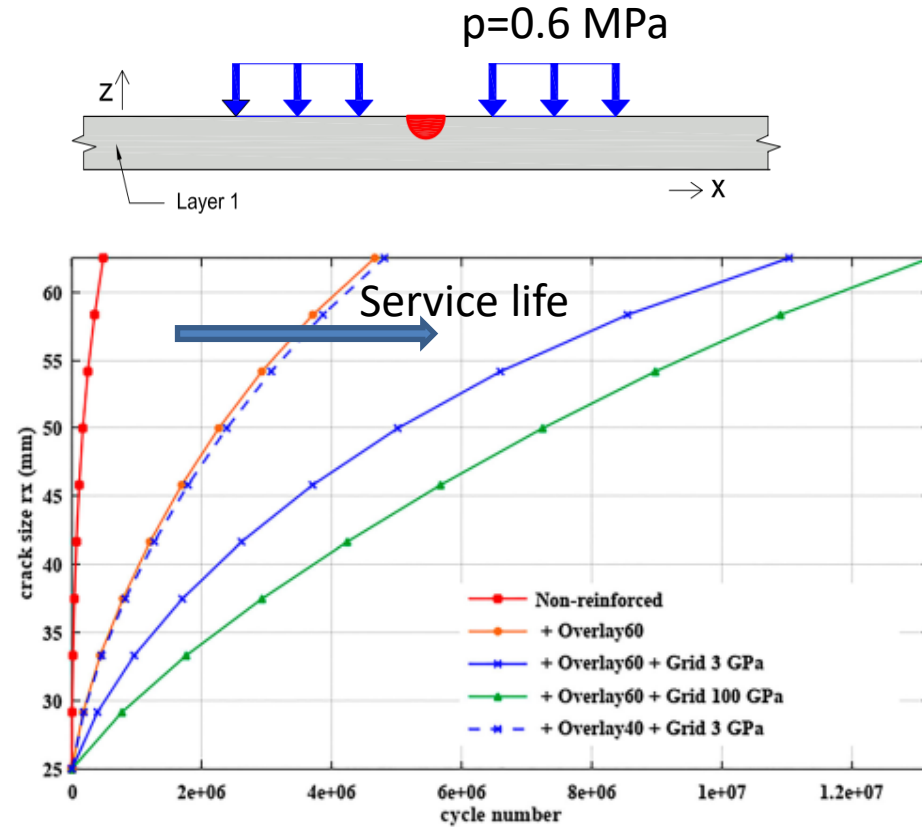
► Simulation of a road pavement with an open crack, grid reinforcement and overlay



20.10<sup>6</sup> cycles

5.10<sup>6</sup> cycles

Mapping the number of cycles based on crack advance



Effects of reinforcements on crack propagation according to X of the crack (diameter 50 mm)



## ► Conclusion and outlook

### ■ Finite element calculations

- For **delamination**: importance of interface, position and surface characteristics
- For **vertical longitudinal (or transverse) cracks**: effect of the crack's position and length on the deflection basin.

The longitudinal deflection measured by a **curvometer type calculation** follows this trend. This calculation is slightly more sensitive (20%/11% (short cracks) - 30%/17% (long cracks)).

- The **maximum relative deflection** (cracked/uncracked comparison) resulting from a theoretical longitudinal measurement (finite element calculation) is **4/100 mm** and that estimated by a curvometer type calculation is of the order of **5/100 mm**.

### ■ Boundary element calculations

- **3D crack path** strongly controlled by the direction of maximum tangential stress
- The model shows **faster crack propagation at the surface** than in the material

### ■ Outlook

- Development of methods relating to the intersection of crack networks and propagation directions
- Search for instrumented experiments or benchmarks

